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# **dnn-locate**

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**dnn-locate** is a Python module for discriminative features localization given a fitted discriminator model, including **neural networks**. **dnn-locate** has the following key features:

1. **Adaptiveness**. For different instances, **dnn-locate** is able to provide **adaptive** discriminative features.
2. **Sparseness**. The discriminative features provided by **dnn-locate** is sparse.
3. *Statistically guaranteed interpretation* in R-square (R<sup>2</sup>). **dnn-locate** is able to *effectively* localize the discriminative features with a target R<sup>2</sup> of prediction.



You can find more information for **dnn-locate**:

- GitHub repo: <https://github.com/statmlben/dnn-inference>

- Documentation: <https://dnn-locate.readthedocs.io>
- PyPi: <https://pypi.org/project/dnn-locate>
- Open Source: [MIT license](#)

## TRUST (TANH RELU SOFTMAX) ACTIVATION FUNCTION

We achieve the (1)-(3) by using the **Magic** activation:  $\tanh + \text{relu} + \text{softmax}$

```
from tensorflow.keras import backend as K

def trust(x, tau, axis_=(1,2)):
    z = tau*K.softmax(x, axis=axis_)
    z = backend.tanh(backend.relu(z))
    return z
```

$\text{trust}(x)$  satisfies that: (i)  $\text{trust}(x) \leq 1$ ; (ii)  $\text{trust}(x) \leq \tau$ , that is, each element is controlled by 1, and the sum of all elements is controlled by  $\tau$ .





## REFERENCE

If you use this code please star the repository and cite the following paper:

```
@article{dai2022locate,  
  title={Data-adaptive discriminative feature localization with statistically_  
↪guaranteed interpretation},  
  author={Dai, Ben and Shen, Xiaotong and Chen, Lin Yee and Li, Chunlin and Pan, Wei},  
  journal={Annals of Applied Statistics},  
  year={2022},  
  publisher={Institute of Mathematical Statistics}  
}
```



## CONTENTS

### 3.1 Installation

#### 3.1.1 Dependencies

dnn-locate requires: **Python**>=3.8 + [pip libs](./requirements.txt)

```
pip install -r requirements.txt
```

#### 3.1.2 User installation

Install dnn-locate using pip

```
pip install dnn_locate
pip install git+https://github.com/statmlben/dnn-locate.git
```

#### 3.1.3 Source code

You can check the latest sources with the command.

```
git clone https://github.com/statmlben/dnn-locate.git
```

### 3.2 Examples

#### 3.2.1 ECG MIT-BIH dataset

**Train ECG localization network**

```
[1]: # Author: Ben Dai
      # Licensed under the Apache License, Version 2.0 (the "License");
      # Train ECG localization network
```

```
[1]: import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import tensorflow as tf
from tensorflow.keras.layers import Dense, Activation, Flatten, Convolution1D, Dropout,
↳MaxPooling1D, GlobalAveragePooling1D
from tensorflow.keras import Model, layers, Sequential, regularizers
from tensorflow.keras.utils import to_categorical
from tensorflow.keras.callbacks import EarlyStopping, ReduceLROnPlateau
from tensorflow.keras.optimizers import Adam
from tensorflow.keras.callbacks import LearningRateScheduler
```

2022-10-14 21:52:36.322750: I tensorflow/core/util/util.cc:169] oneDNN custom operations\_
↳are on. You may see slightly different numerical results due to floating-point round-
↳off errors from different computation orders. To turn them off, set the environment\_
↳variable `TF\_ENABLE\_ONEDNN\_OPTS=0`.

```
[2]: ## Load data and pretrained model

discriminator=tf.keras.models.load_model('./tests/ECG_model/pretrained_model.h5')
# discriminator.summary()

mit_train_path="./dataset/mitbih_train.csv"
mit_test_path="./dataset/mitbih_test.csv"

def create_pd(train_path,test_path):
    train=pd.read_csv(train_path)
    test=pd.read_csv(test_path)
    train.columns=[x for x in range(188)]
    test.columns=[x for x in range(188)]
    return pd.concat([train,test], axis=0, join='inner').sort_index()

mit= create_pd(mit_train_path,mit_test_path)

X = np.asarray(mit.iloc[:, :187].values)
y = mit.iloc[:, 187].values
y = to_categorical(y)

X = X.reshape(-1, 187, 1)
input_shape = X.shape[1:]

from sklearn.model_selection import train_test_split
X, X_test, y, y_test = train_test_split(X, y, test_size=0.33, random_state=42)
```

2022-10-14 21:52:39.025442: I tensorflow/stream\_executor/cuda/cuda\_gpu\_executor.cc:975]\_
↳successful NUMA node read from SysFS had negative value (-1), but there must be at\_
↳least one NUMA node, so returning NUMA node zero

2022-10-14 21:52:39.030579: I tensorflow/stream\_executor/cuda/cuda\_gpu\_executor.cc:975]\_
↳successful NUMA node read from SysFS had negative value (-1), but there must be at\_
↳least one NUMA node, so returning NUMA node zero

2022-10-14 21:52:39.030931: I tensorflow/stream\_executor/cuda/cuda\_gpu\_executor.cc:975]\_
↳successful NUMA node read from SysFS had negative value (-1), but there must be at\_
↳least one NUMA node, so returning NUMA node zero

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```

2022-10-14 21:52:39.031751: I tensorflow/core/platform/cpu_feature_guard.cc:193] This
→TensorFlow binary is optimized with oneAPI Deep Neural Network Library (oneDNN) to use
→the following CPU instructions in performance-critical operations:  AVX2 AVX512F
→AVX512_VNNI FMA
To enable them in other operations, rebuild TensorFlow with the appropriate compiler
→flags.
2022-10-14 21:52:39.032337: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:975]
→successful NUMA node read from SysFS had negative value (-1), but there must be at
→least one NUMA node, so returning NUMA node zero
2022-10-14 21:52:39.032622: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:975]
→successful NUMA node read from SysFS had negative value (-1), but there must be at
→least one NUMA node, so returning NUMA node zero
2022-10-14 21:52:39.032886: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:975]
→successful NUMA node read from SysFS had negative value (-1), but there must be at
→least one NUMA node, so returning NUMA node zero
2022-10-14 21:52:39.390903: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:975]
→successful NUMA node read from SysFS had negative value (-1), but there must be at
→least one NUMA node, so returning NUMA node zero
2022-10-14 21:52:39.391197: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:975]
→successful NUMA node read from SysFS had negative value (-1), but there must be at
→least one NUMA node, so returning NUMA node zero
2022-10-14 21:52:39.391438: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:975]
→successful NUMA node read from SysFS had negative value (-1), but there must be at
→least one NUMA node, so returning NUMA node zero
2022-10-14 21:52:39.391670: I tensorflow/core/common_runtime/gpu/gpu_device.cc:1532]
→Created device /job:localhost/replica:0/task:0/device:GPU:0 with 3647 MB memory:  ->
→device: 0, name: NVIDIA GeForce RTX 2060, pci bus id: 0000:01:00.0, compute capability:
→ 7.5

```

```

[3]: ## Model
from dnn_locate import loc_model
## define the backend localizer before TRELU activation

localizer_backend = tf.keras.Sequential(
    [
        layers.Input(shape=(input_shape[0], input_shape[1])),
        layers.Conv1D(
            filters=32, kernel_size=5, padding="same", strides=1, activation="relu"
        ),
        layers.Dropout(rate=0.2),
        layers.Conv1D(
            filters=16, kernel_size=5, padding="same", strides=1, activation="relu"
        ),
        layers.Conv1DTranspose(
            filters=16, kernel_size=5, padding="same", strides=1, activation="relu"
        ),
        layers.Dropout(rate=0.2),
        layers.Conv1DTranspose(
            filters=32, kernel_size=5, padding="same", strides=1, activation="relu"
        ),
        layers.Conv1DTranspose(filters=1, kernel_size=5, padding="same"),
    ]

```

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```

)

es_detect1 = ReduceLROnPlateau(monitor="loss", factor=0.382, min_lr=1e-6,
                               verbose=1, patience=3, mode="min")
es_detect2 = EarlyStopping(monitor='loss', mode='min', min_delta=.0001,
                           verbose=1, patience=10, restore_best_weights=True)

fit_params={'callbacks': [es_detect1, es_detect2],
            'epochs': 100, 'batch_size': 64}

tau_range = [10., 20, 30]

## define framework
cue = loc_model(input_shape=input_shape,
                 localizer_backend=localizer_backend,
                 discriminator=discriminator,
                 target_r_square='auto',
                 r_metric='acc',
                 # r_metric='loss',
                 tau_range=tau_range)

/home/ben/tf/lib/python3.10/site-packages/keras/optimizers/optimizer_v2/gradient_descent.
↳ py:108: UserWarning: The `lr` argument is deprecated, use `learning_rate` instead.
    super(SGD, self).__init__(name, **kwargs)

```

```

[4]: cue.fit(X_train=X, y_train=y,
            fit_params=fit_params,
            optimizer=Adam(learning_rate=.01)
            # optimizer=SGDW(learning_rate=.1, weight_decay=.0001, momentum=.9)
            )

```

```

2022-10-14 21:52:44.663196: I tensorflow/stream_executor/cuda/cuda_dnn.cc:384] Loaded
↳ cuDNN version 8101

```

```

2292/2292 [=====] - 4s 1ms/step - loss: 0.0483 - accuracy: 0.
↳ 9861 - auc: 0.9990
2292/2292 [=====] - 3s 1ms/step - loss: 5.1039 - accuracy: 0.
↳ 7042 - auc: 0.8160
Epoch 1/100
1146/1146 [=====] - 7s 5ms/step - loss: -5.3217 - lr: 0.0100
Epoch 2/100
1146/1146 [=====] - 4s 4ms/step - loss: -7.3224 - lr: 0.0100
Epoch 3/100
1146/1146 [=====] - 4s 4ms/step - loss: -7.9352 - lr: 0.0100
Epoch 4/100
1146/1146 [=====] - 4s 4ms/step - loss: -8.1900 - lr: 0.0100
Epoch 5/100
1146/1146 [=====] - 4s 4ms/step - loss: -8.1250 - lr: 0.0100
Epoch 6/100
1146/1146 [=====] - 4s 4ms/step - loss: -8.2364 - lr: 0.0100
Epoch 7/100
1146/1146 [=====] - 4s 4ms/step - loss: -8.4304 - lr: 0.0100

```

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```

Epoch 8/100
1146/1146 [=====] - 4s 4ms/step - loss: -8.7386 - lr: 0.0100
Epoch 9/100
1146/1146 [=====] - 5s 4ms/step - loss: -8.6743 - lr: 0.0100
Epoch 10/100
1146/1146 [=====] - 4s 4ms/step - loss: -8.7296 - lr: 0.0100
Epoch 11/100
1146/1146 [=====] - 4s 4ms/step - loss: -8.8596 - lr: 0.0100
Epoch 12/100
1146/1146 [=====] - 4s 4ms/step - loss: -8.9157 - lr: 0.0100
Epoch 13/100
1146/1146 [=====] - 4s 4ms/step - loss: -8.7552 - lr: 0.0100
Epoch 14/100
1146/1146 [=====] - 4s 4ms/step - loss: -9.0108 - lr: 0.0100
Epoch 15/100
1146/1146 [=====] - 4s 4ms/step - loss: -8.7194 - lr: 0.0100
Epoch 16/100
1146/1146 [=====] - 4s 4ms/step - loss: -9.1780 - lr: 0.0100
Epoch 17/100
1146/1146 [=====] - 4s 4ms/step - loss: -9.0624 - lr: 0.0100
Epoch 18/100
1146/1146 [=====] - 4s 4ms/step - loss: -9.2963 - lr: 0.0100
Epoch 19/100
1146/1146 [=====] - 4s 4ms/step - loss: -9.2474 - lr: 0.0100
Epoch 20/100
1146/1146 [=====] - 4s 4ms/step - loss: -9.2477 - lr: 0.0100
Epoch 21/100
1146/1146 [=====] - 4s 4ms/step - loss: -9.3848 - lr: 0.0100
Epoch 22/100
1146/1146 [=====] - 4s 4ms/step - loss: -9.4511 - lr: 0.0100
Epoch 23/100
1146/1146 [=====] - 4s 4ms/step - loss: -9.5072 - lr: 0.0100
Epoch 24/100
1146/1146 [=====] - 4s 4ms/step - loss: -9.4762 - lr: 0.0100
Epoch 25/100
1146/1146 [=====] - 4s 4ms/step - loss: -9.5786 - lr: 0.0100
Epoch 26/100
1146/1146 [=====] - 5s 4ms/step - loss: -9.6250 - lr: 0.0100
Epoch 27/100
1146/1146 [=====] - 5s 4ms/step - loss: -9.3385 - lr: 0.0100
Epoch 28/100
1146/1146 [=====] - 4s 4ms/step - loss: -9.3302 - lr: 0.0100
Epoch 29/100
1140/1146 [=====>.] - ETA: 0s - loss: -9.5342
Epoch 29: ReduceLROnPlateau reducing learning rate to 0.0038199999146163463.
1146/1146 [=====] - 4s 4ms/step - loss: -9.5332 - lr: 0.0100
Epoch 30/100
1146/1146 [=====] - 4s 4ms/step - loss: -9.8781 - lr: 0.0038
Epoch 31/100
1146/1146 [=====] - 4s 4ms/step - loss: -9.9837 - lr: 0.0038
Epoch 32/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.1294 - lr: 0.0038

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```

Epoch 33/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.1395 - lr: 0.0038
Epoch 34/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.1378 - lr: 0.0038
Epoch 35/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.0610 - lr: 0.0038
Epoch 36/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.1958 - lr: 0.0038
Epoch 37/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.2177 - lr: 0.0038
Epoch 38/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.1821 - lr: 0.0038
Epoch 39/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.2419 - lr: 0.0038
Epoch 40/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.1798 - lr: 0.0038
Epoch 41/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.2267 - lr: 0.0038
Epoch 42/100
1139/1146 [=====>.] - ETA: 0s - loss: -10.2399
Epoch 42: ReduceLRonPlateau reducing learning rate to 0.0014592399937100708.
1146/1146 [=====] - 4s 4ms/step - loss: -10.2379 - lr: 0.0038
Epoch 43/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.2871 - lr: 0.0015
Epoch 44/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.4394 - lr: 0.0015
Epoch 45/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.4516 - lr: 0.0015
Epoch 46/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.4511 - lr: 0.0015
Epoch 47/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.4310 - lr: 0.0015
Epoch 48/100
1137/1146 [=====>.] - ETA: 0s - loss: -10.4450
Epoch 48: ReduceLRonPlateau reducing learning rate to 0.0005574296731501818.
1146/1146 [=====] - 4s 4ms/step - loss: -10.4506 - lr: 0.0015
Epoch 49/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.5040 - lr: 5.5743e-
↪ 04
Epoch 50/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.5365 - lr: 5.5743e-
↪ 04
Epoch 51/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.4818 - lr: 5.5743e-
↪ 04
Epoch 52/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.4441 - lr: 5.5743e-
↪ 04
Epoch 53/100
1146/1146 [=====] - ETA: 0s - loss: -10.4994
Epoch 53: ReduceLRonPlateau reducing learning rate to 0.00021293813816737384.
1146/1146 [=====] - 4s 4ms/step - loss: -10.4994 - lr: 5.5743e-

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↪04
Epoch 54/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.5423 - lr: 2.1294e-
↪04
Epoch 55/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.5513 - lr: 2.1294e-
↪04
Epoch 56/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.5156 - lr: 2.1294e-
↪04
Epoch 57/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.5144 - lr: 2.1294e-
↪04
Epoch 58/100
1136/1146 [=====>.] - ETA: 0s - loss: -10.5268
Epoch 58: ReduceLRonPlateau reducing learning rate to 8.134236637852155e-05.
1146/1146 [=====] - 4s 4ms/step - loss: -10.5221 - lr: 2.1294e-
↪04
Epoch 59/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.5352 - lr: 8.1342e-
↪05
Epoch 60/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.5340 - lr: 8.1342e-
↪05
Epoch 61/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.5820 - lr: 8.1342e-
↪05
Epoch 62/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.5997 - lr: 8.1342e-
↪05
Epoch 63/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.5458 - lr: 8.1342e-
↪05
Epoch 64/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.5407 - lr: 8.1342e-
↪05
Epoch 65/100
1145/1146 [=====>.] - ETA: 0s - loss: -10.5950
Epoch 65: ReduceLRonPlateau reducing learning rate to 3.107278476818465e-05.
1146/1146 [=====] - 4s 4ms/step - loss: -10.5960 - lr: 8.1342e-
↪05
Epoch 66/100
1146/1146 [=====] - 5s 4ms/step - loss: -10.5197 - lr: 3.1073e-
↪05
Epoch 67/100
1146/1146 [=====] - 5s 4ms/step - loss: -10.5252 - lr: 3.1073e-
↪05
Epoch 68/100
1146/1146 [=====] - 5s 4ms/step - loss: -10.6115 - lr: 3.1073e-
↪05
Epoch 69/100
1146/1146 [=====] - 5s 4ms/step - loss: -10.5617 - lr: 3.1073e-

```

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```

→05
Epoch 70/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.6030 - lr: 3.1073e-
→05
Epoch 71/100
1146/1146 [=====] - ETA: 0s - loss: -10.5464
Epoch 71: ReduceLROnPlateau reducing learning rate to 1.1869803725858219e-05.
1146/1146 [=====] - 4s 4ms/step - loss: -10.5464 - lr: 3.1073e-
→05
Epoch 72/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.6003 - lr: 1.1870e-
→05
Epoch 73/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.5594 - lr: 1.1870e-
→05
Epoch 74/100
1133/1146 [=====>.] - ETA: 0s - loss: -10.5983
Epoch 74: ReduceLROnPlateau reducing learning rate to 4.534264948233613e-06.
1146/1146 [=====] - 4s 4ms/step - loss: -10.6071 - lr: 1.1870e-
→05
Epoch 75/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.5452 - lr: 4.5343e-
→06
Epoch 76/100
1146/1146 [=====] - 4s 4ms/step - loss: -10.5684 - lr: 4.5343e-
→06
Epoch 77/100
1143/1146 [=====>.] - ETA: 0s - loss: -10.5494
Epoch 77: ReduceLROnPlateau reducing learning rate to 1.7320891984127228e-06.
1146/1146 [=====] - 4s 4ms/step - loss: -10.5420 - lr: 4.5343e-
→06
Epoch 78/100
1137/1146 [=====>.] - ETA: 0s - loss: -10.5708Restoring model_
→weights from the end of the best epoch: 68.
1146/1146 [=====] - 4s 4ms/step - loss: -10.5738 - lr: 1.7321e-
→06
Epoch 78: early stopping
#####
compute the R2 for the fitted localizer.
#####
2292/2292 [=====] - 3s 1ms/step - loss: 0.0483 - accuracy: 0.
→9861 - auc: 0.9990
2292/2292 [=====] - 2s 945us/step
2292/2292 [=====] - 3s 1ms/step - loss: 11.0031 - accuracy: 0.
→1729 - auc: 0.4940
1/1 [=====] - 0s 92ms/step
early stop in tau = 10.000, R2: 0.983; target R2: 0.953 is reached

```

```

[5]: ## print R_square for Test set
cue.R_square(X_test, y_test)

```

```
#####
```

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```

compute the R2 for the fitted localizer.
#####
1129/1129 [=====] - 2s 2ms/step - loss: 0.0455 - accuracy: 0.
↪9862 - auc: 0.9992
1129/1129 [=====] - 1s 939us/step
1129/1129 [=====] - 2s 1ms/step - loss: 11.0295 - accuracy: 0.
↪1713 - auc: 0.4927

```

```
[5]: 0.9833611752340135
```

```

[6]: ## Plot the localization results by the fitted network for novel instances
import seaborn as sns
import matplotlib

import matplotlib.pyplot as plt

n_label = y.shape[1]
cmap = ["Oranges", "Purples", "Reds", "Blues", "Greens"]
c1 = ['darkorange', 'darkslateblue', 'darkred', 'darkblue', 'darkgreen']
c2 = ['darkgreen', 'darkred', 'darkslateblue', 'darkred', 'darkorange']

n_demo = 3
timepoint = list(range(input_shape[0]))

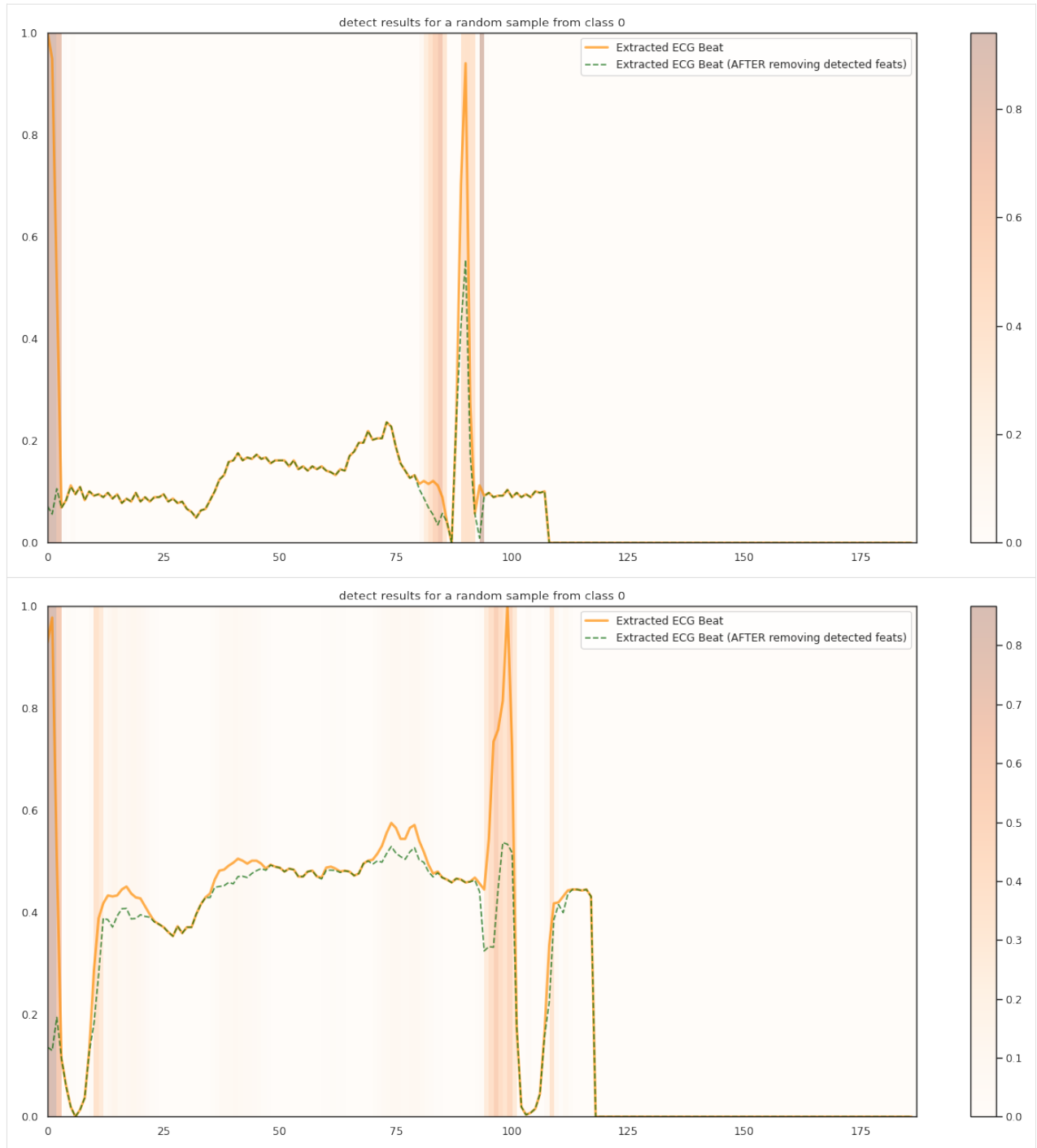
for k in range(n_label):
    demo_ind = np.array([np.random.choice(np.where(y_test[:,k] == 1)[0]) for i in
↪range(n_demo)])
    X_demo = X_test[demo_ind]
    X_demo_detect = cue.localizer.predict(X_demo)
    X_demo_hl = cue.locate(X_demo)

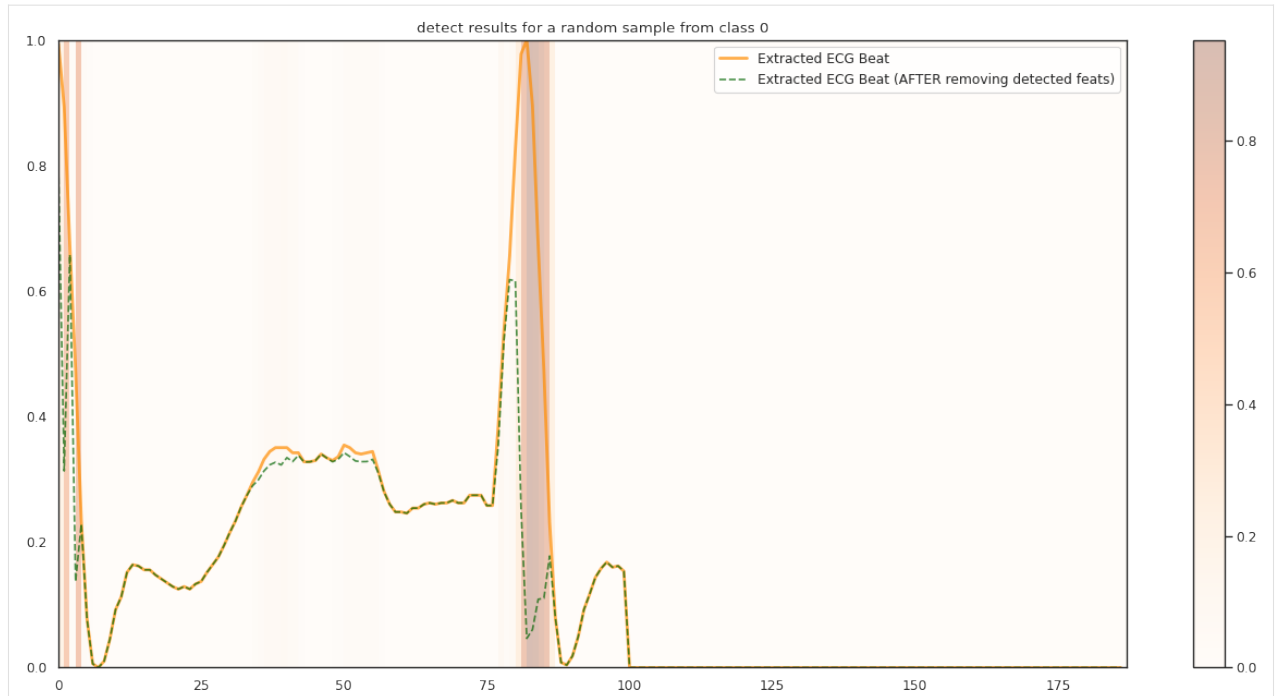
    sns.set_theme(style='white', palette=None)
    for i in range(len(X_demo)):
        X_tmp, X_detect_tmp, X_hl_tmp = X_demo[i], X_demo_detect[i], X_demo_hl[i]
        plt.figure(figsize=(16, 8), dpi=80)
        plt.title('detect results for a random sample from class %s' %k)
        plt.imshow(X_hl_tmp[np.newaxis,:], cmap=cmap[k], aspect='auto', alpha=0.3,
↪extent = (0, 187, 0, 1))

        plt.colorbar()
        plt.plot(timepoint, X_tmp, linewidth=2.5, alpha=.7, color=c1[k],
↪label='Extracted ECG Beat')
        plt.plot(timepoint, X_detect_tmp, linewidth=1.5, alpha=.7, color=c2[k],
↪linestyle='--',
↪label='Extracted ECG Beat (AFTER removing detected feats)')
        plt.legend(loc='best')
        plt.tight_layout()
        plt.show()

1/1 [=====] - 0s 101ms/step
1/1 [=====] - 0s 12ms/step

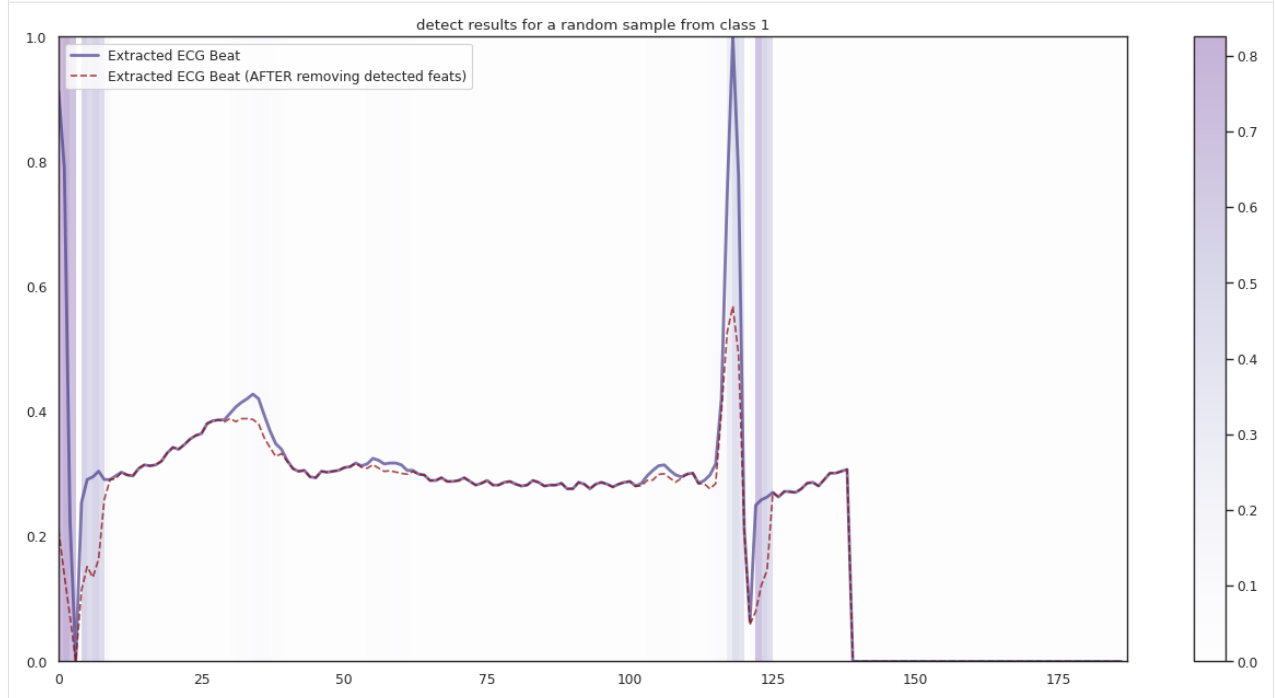
```

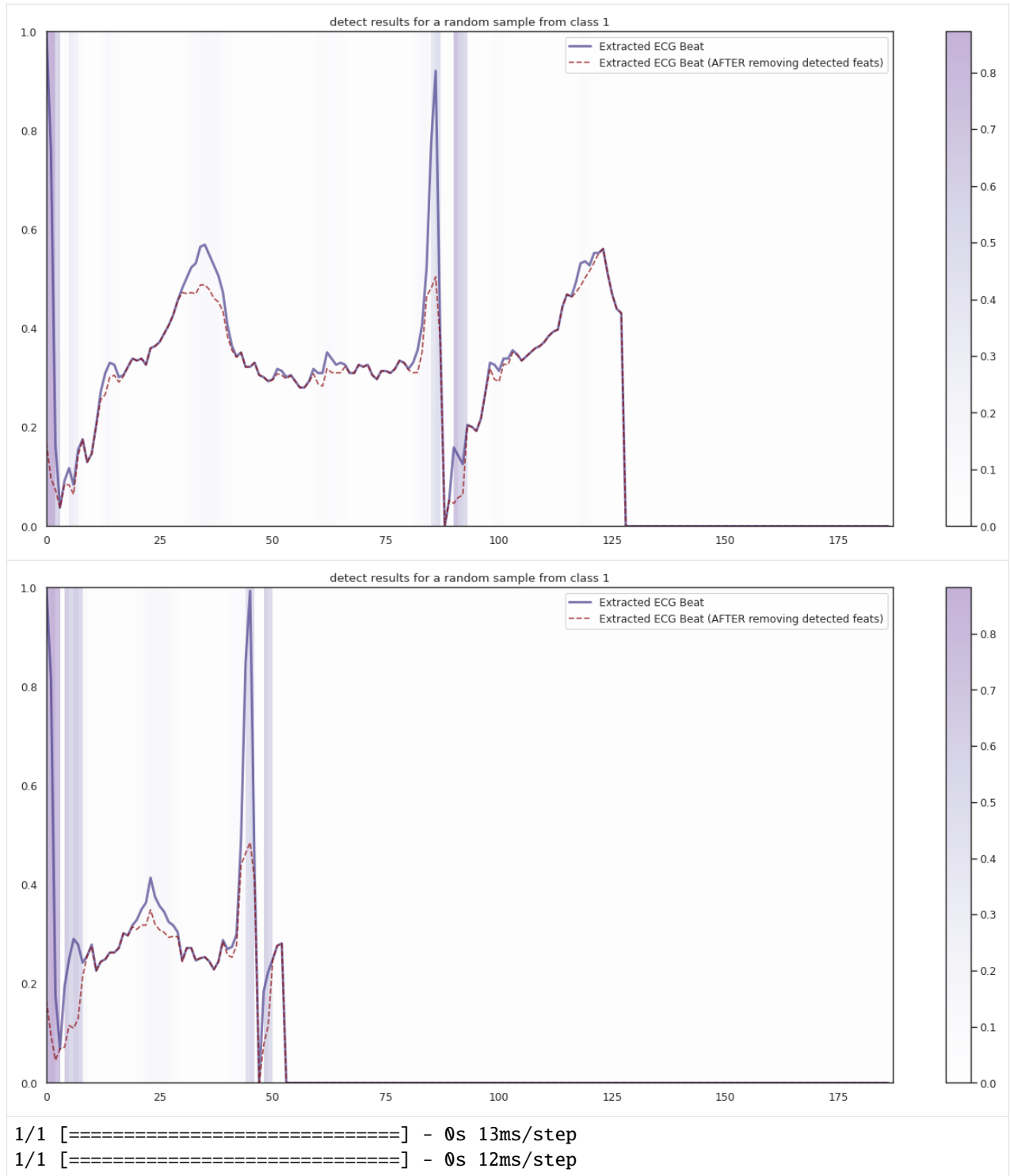


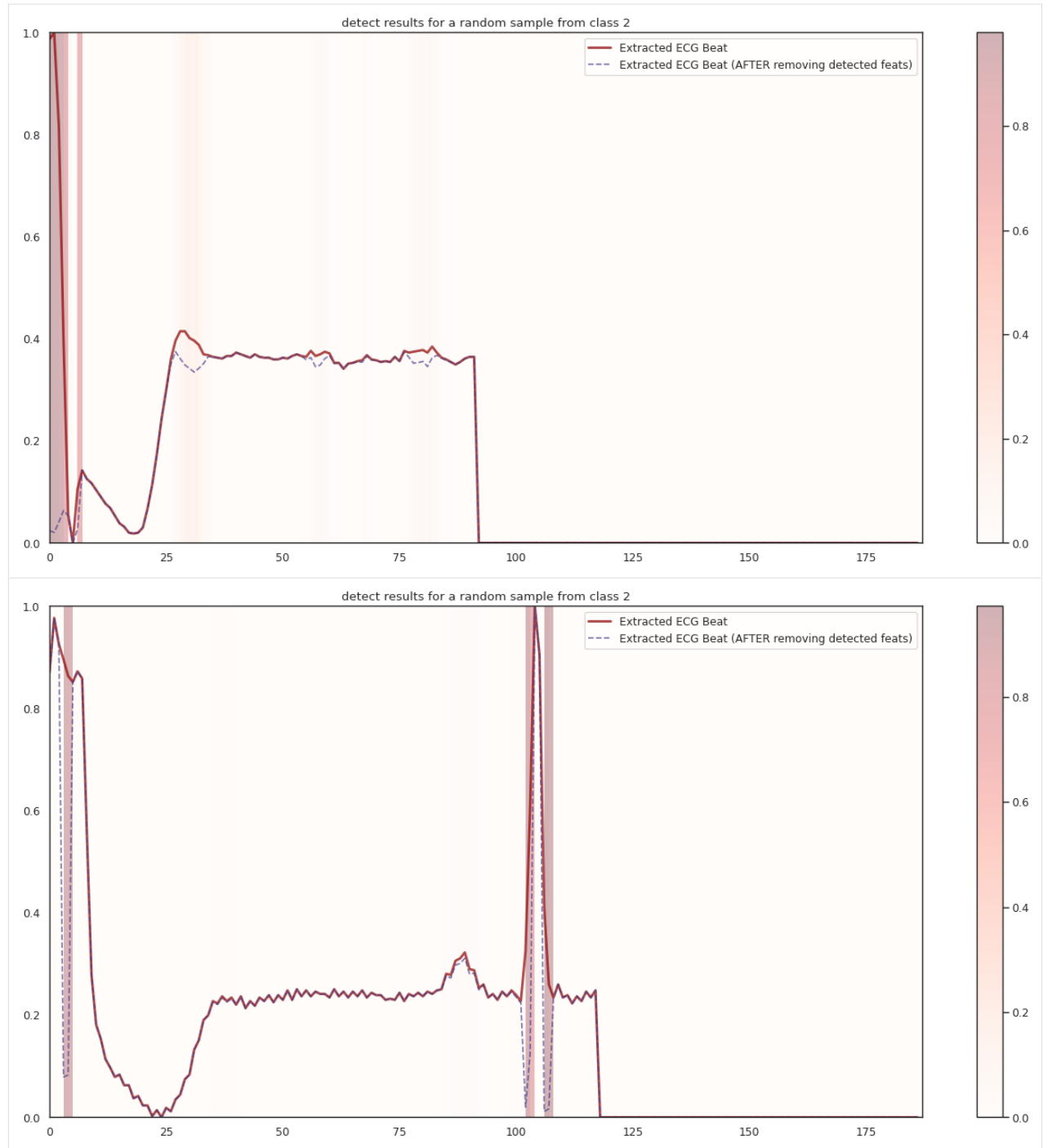


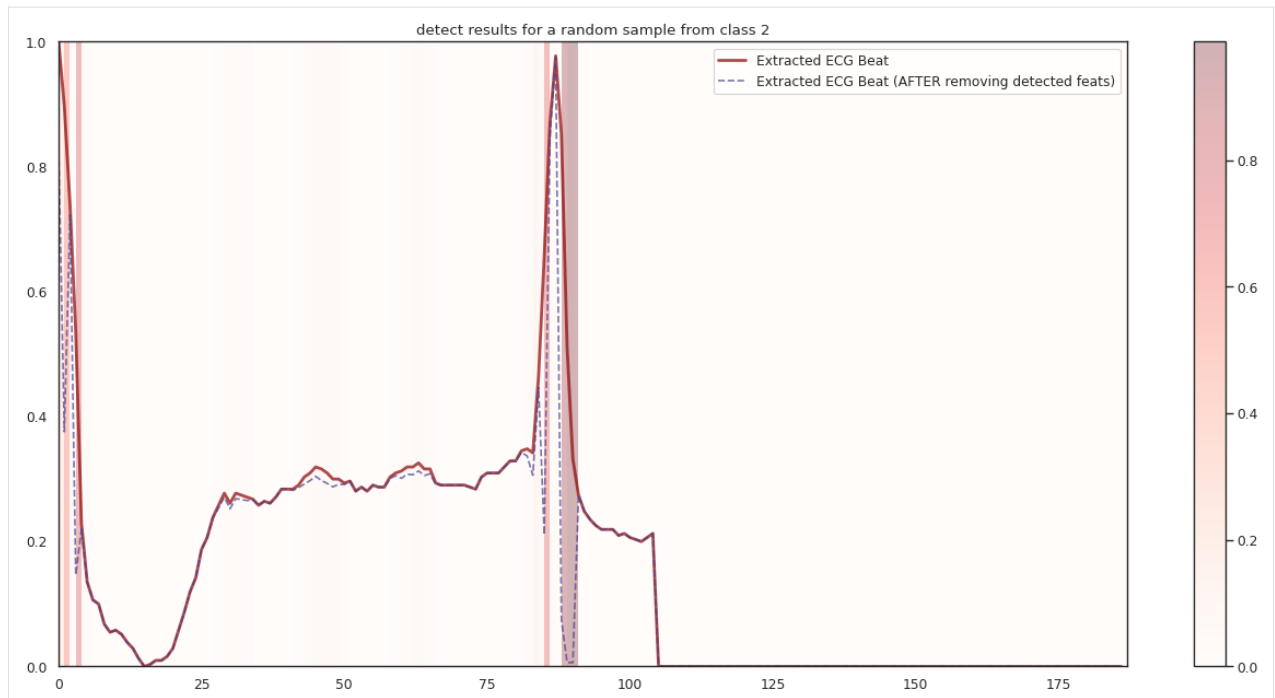
1/1 [=====] - 0s 13ms/step

1/1 [=====] - 0s 12ms/step



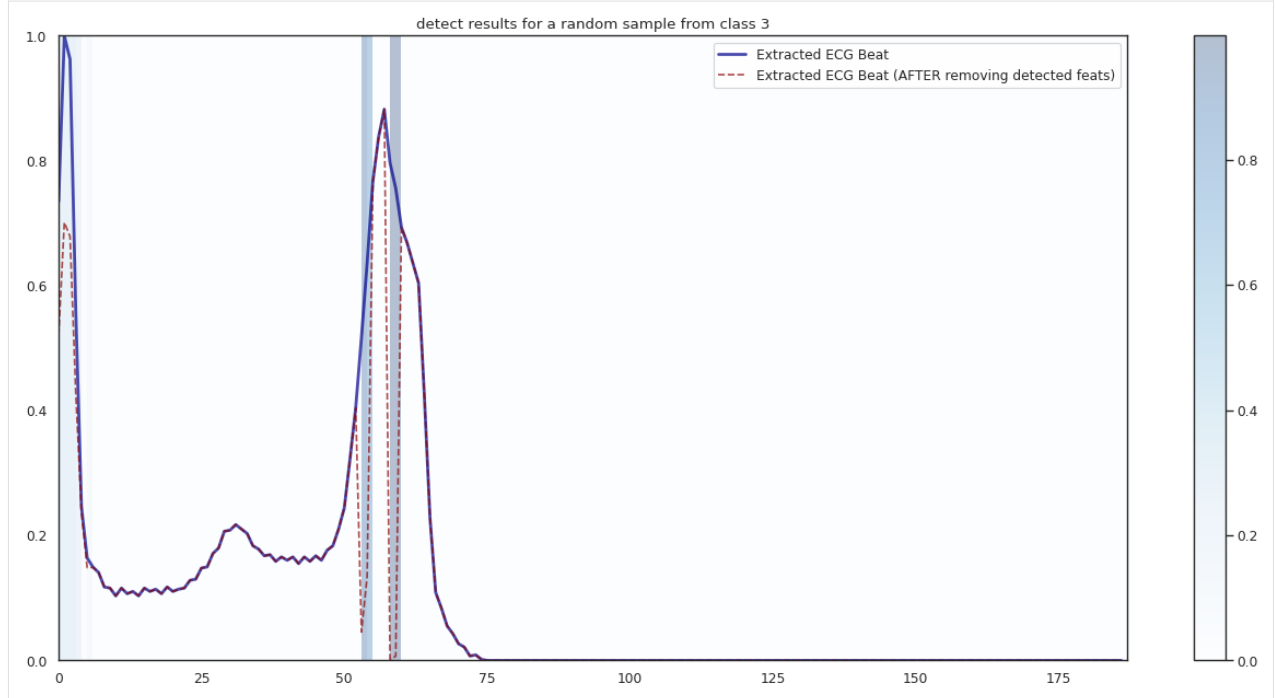




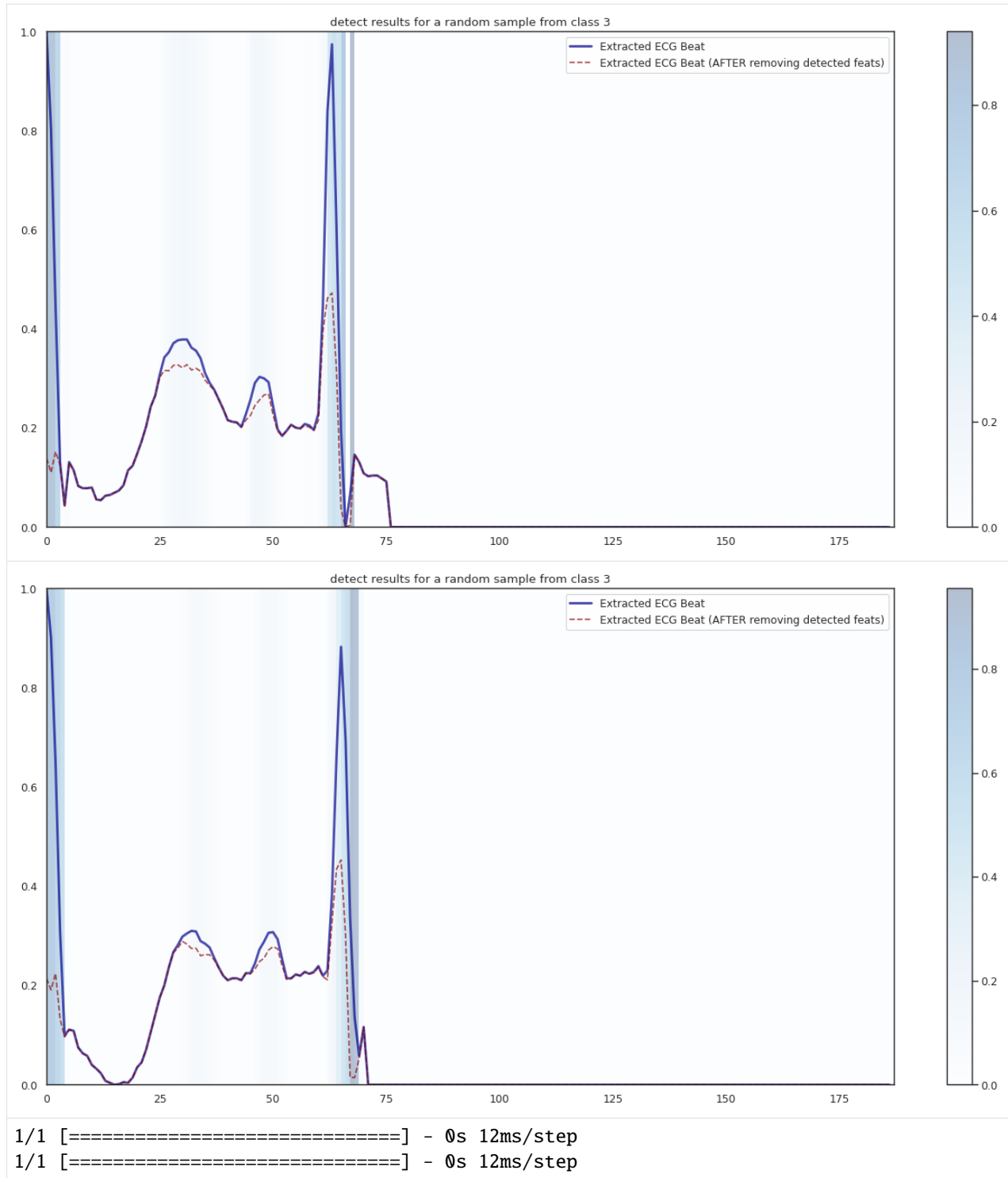


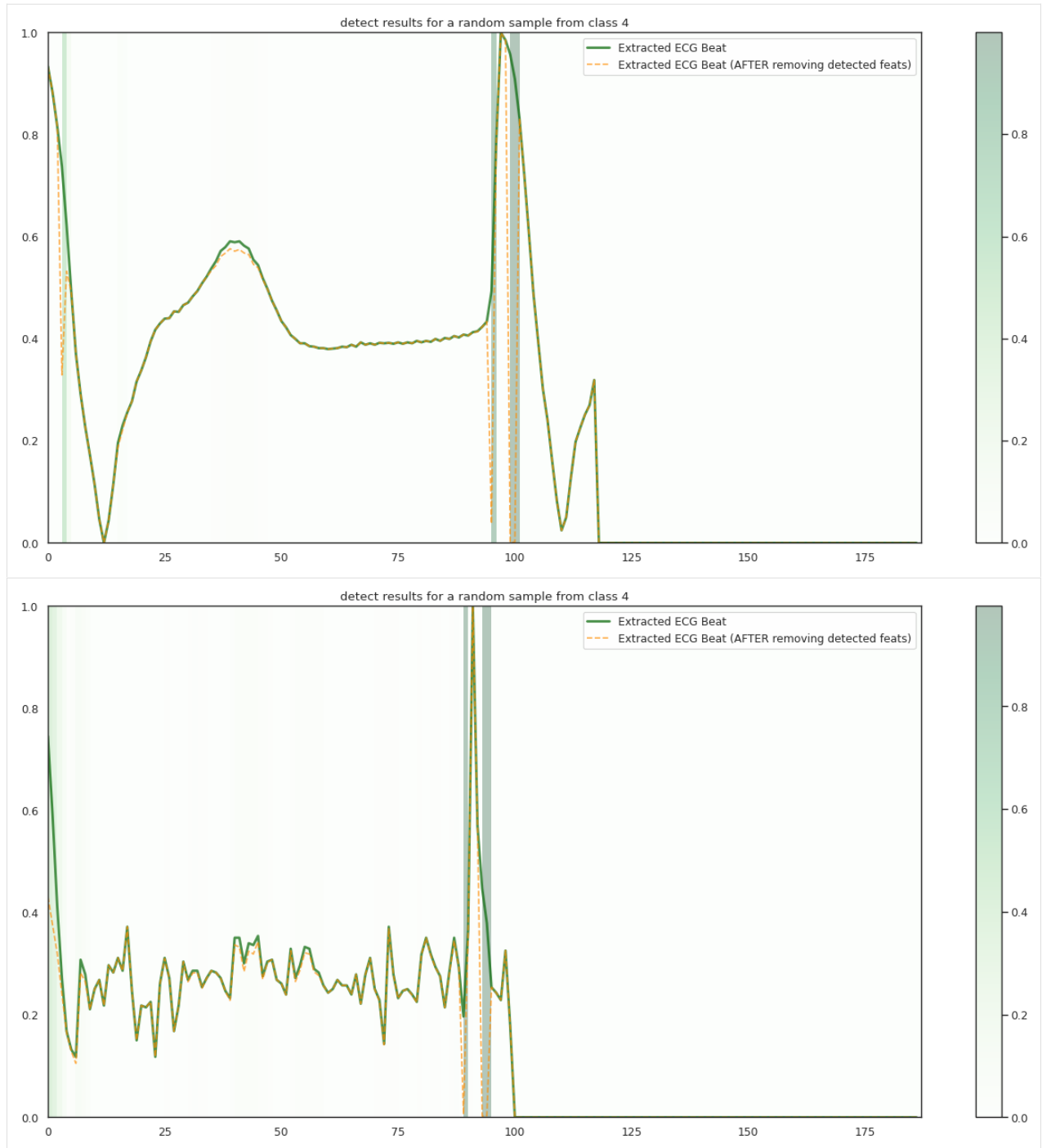
1/1 [=====] - 0s 14ms/step

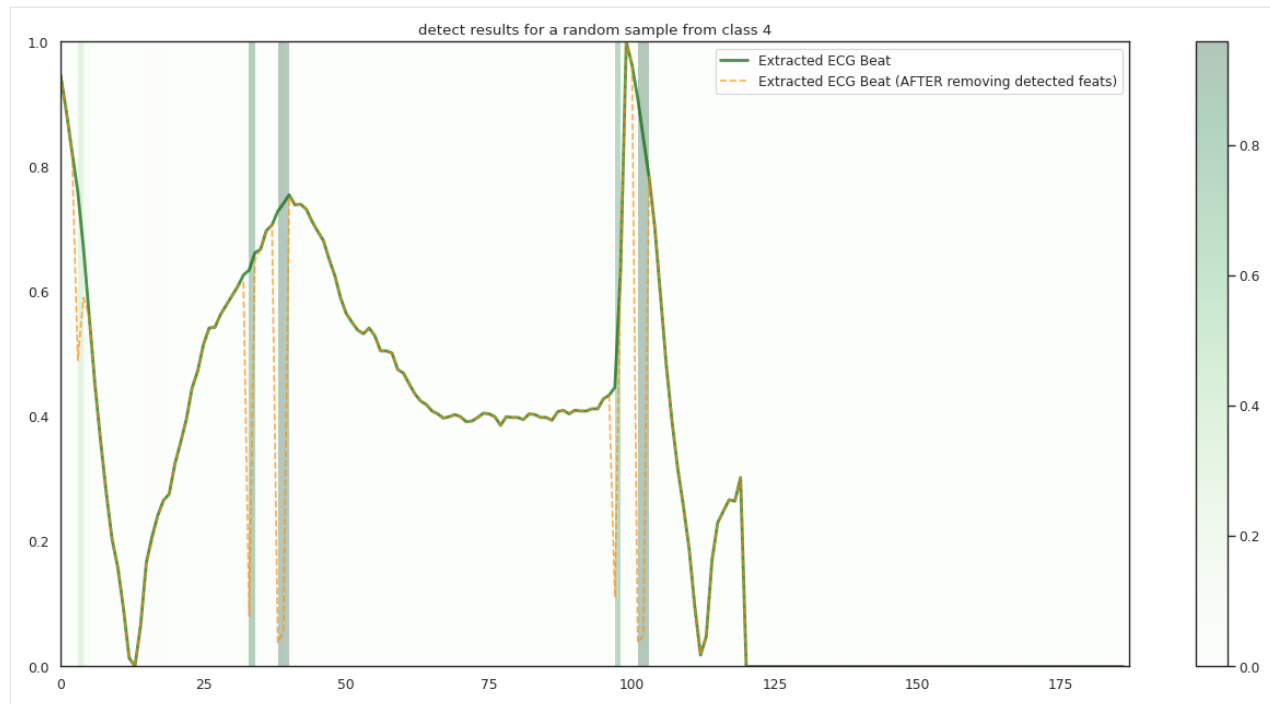
1/1 [=====] - 0s 12ms/step











## Results

- The localized regions of ECG complexes in sinus rhythm are most informative in distinguishing presence of ventricular ectopic beats from supraventricular ectopic beats in a particular individual. The localized regions lie in the **QRS complex**, which correlates with ventricular depolarization or electrical propagation in the ventricles. Ion channel aberrations and structural abnormalities in the ventricles can affect electrical conduction in the ventricles, manifesting with subtle anomalies in the QRS complex in sinus rhythm that **may not be discernible by the naked eye but is detectable by the convolutional auto-encoder**. Of note, as the  $R^2$  increases from 10% to 88%, the highlighted color bar is progressively broader, covering a higher proportion of the QRS complex. The foregoing observations are sensible: the regions of interest resided in the QRS complex are biologically plausible and **consistent with cardiac electrophysiological principles**.
- As the  $R^2$  increases from 80% to 84% and finally 88%, the blue bar progressively highlights the P wave of ECG complexes in sinus rhythm. This observation is **consistent with our understanding of the mechanistic underpinnings of atrial depolarization**, which correlates with the P wave. Ion channel alterations and structural changes in the atria can affect electrical conduction in the atria manifesting with subtle anomalies in the P wave in sinus rhythm that may not be discernible by the naked eye but are detectable by the convolutional auto-encoder.
- Collectively, the examples underscore the fact that the discriminative regions of interest identified by our proposed method are biologically plausible and consistent with cardiac electrophysiological principles while **locating subtle anomalies in the P wave and QRS complex that may not be discernible by the naked eye**. By inspecting our results with an ECG clinician [Dr. Lin Yee Chen](#), the localized discriminative features of the ECG are consistent with medical interpretation in ECG diagnosis.

### 3.2.2 MNIST dataset

#### Train MNIST localization network

```
[2]: from keras.datasets import mnist
      from keras.optimizers import Adam, SGD
      from keras.callbacks import EarlyStopping, ReduceLROnPlateau

      from dnn_locate import Dnn_Locate
      import matplotlib.pyplot as plt
      import numpy as np
      import tensorflow as tf

[3]: ## load data
      np.random.seed(3)
      tf.random.set_seed(3)

      input_shape, labels = (28, 28, 1), 10

      ## load data
      (X_train, y_train), (X_test, y_test) = mnist.load_data()
      X_train = X_train / 255.
      X_test = X_test / 255.

      ind_set = np.array([i for i in range(len(y_train)) if y_train[i] in [7, 9]])
      ind_set_test = np.array([i for i in range(len(y_test)) if y_test[i] in [7, 9]])

      X_train, y_train = X_train[ind_set], y_train[ind_set]
      X_test, y_test = X_test[ind_set_test], y_test[ind_set_test]

      X_train = np.expand_dims(X_train, axis=3)
      X_test = np.expand_dims(X_test, axis=3)

[ ]: ## define models
      from keras import initializers
      from keras.models import Sequential, Model
      from keras.layers import UpSampling2D, Conv2D
      from keras.layers import Input, Dense, Reshape, Flatten, Dropout, Add, Multiply,
      ↪ Conv2DTranspose
      from keras.layers import BatchNormalization, Activation, ZeroPadding2D, MaxPooling2D,
      ↪ GlobalAveragePooling2D

      initializer = initializers.glorot_uniform(seed=0)

      ## define the detector before TRELU activation
      detector = Sequential()
      detector.add(Conv2D(32, (2,2),
          padding="same",
          input_shape=input_shape,
          kernel_initializer=initializer,
          bias_initializer=initializer))
      detector.add(Flatten())
```

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```

detector.add(Dense(128, activation='relu',
    kernel_initializer=initializer,
    bias_initializer=initializer))
detector.add(Dense(128, activation='relu',
    kernel_initializer=initializer,
    bias_initializer=initializer))
detector.add(Dense(np.prod(input_shape),
    activation='softmax',
    kernel_initializer=initializer,
    bias_initializer=initializer))
detector.add(Reshape(input_shape))

## define discriminator
discriminator = Sequential()
discriminator.add(Conv2D(32, (3, 3),
    activation='relu', name='last_conv',
    kernel_initializer=initializer,
    bias_initializer=initializer,
    kernel_regularizer=tf.keras.regularizers.l1(0.001),
    bias_regularizer=tf.keras.regularizers.l1(0.001),
    input_shape=input_shape))
discriminator.add(MaxPooling2D((2, 2)))
discriminator.add(Flatten())
discriminator.add(Dense(100, activation='relu',
    kernel_regularizer=tf.keras.regularizers.l1(0.001),
    bias_regularizer=tf.keras.regularizers.l1(0.001),
    kernel_initializer=initializer))
discriminator.add(Dense(labels, activation='softmax',
    kernel_initializer=initializer,
    kernel_regularizer=tf.keras.regularizers.l1(0.001),
    bias_regularizer=tf.keras.regularizers.l1(0.001),
    bias_initializer=initializer))
discriminator.compile(loss='sparse_categorical_crossentropy',
    optimizer=Adam(lr=0.001),
    metrics=['accuracy'])

```

```

[ ]: ## define framework
tau_range = [4., 6., 8., 10., 12., 14., 16., ]
shiing = Dnn_Locate(input_shape=input_shape,
    discriminator=discriminator,
    tau_range=tau_range,
    task='classification')

es_detect1 = ReduceLROnPlateau(monitor="loss", factor=0.382, min_lr=.0001,
    verbose=1, patience=5, mode="min")
es_detect2 = EarlyStopping(monitor='loss', mode='min', min_delta=.0001,
    verbose=1, patience=15, restore_best_
    ↪ weights=True)
es_learn = EarlyStopping(monitor='val_accuracy', mode='max',
    verbose=1, patience=10, restore_best_
    ↪ weights=True)

```

```
[ ]: print('###'*20)
print('###'*5+' '*6+'Load learner'+ ' '*5+'###'*5)
print('###'*20)

# learn_tmp = shiing.discriminator.fit(x=X_train, y=y_train, callbacks=[es_learn],
↳ epochs=50, batch_size=128, validation_split=.2)
# shiing.discriminator.save_weights("./saved_model/model1107.h5")
# shiing.discriminator.load_weights("./saved_model/model1107.h5")
shiing.discriminator.load_weights("../tests/saved_model/model1119.h5")
# shiing.discriminator.load_weights("./saved_model/model1126.h5")

print('###'*20)
print('#'*16+' '*5+'Train detector'+ ' '*5+'#'*16)
print('###'*20)

## fit detector for a range of tau
fit_params={'callbacks': [es_detect1, es_detect2],
            'epochs': 1000, 'batch_size': 64}

shiing.fit(X_train=X_train, y_train=y_train, detector=detector,
           optimizer=SGD(lr=1.), fit_params=fit_params)

[ ]: ## Visualize the results
shiing.R_sqaure_path()
shiing.path_plot()
shiing.DA_plot(X=X_test, y=y_test)
```

## 3.3 API Reference

### 3.3.1 dnn\_locate.loc\_model

#### loc\_model

```
class dnn_locate.loc_model.loc_model(input_shape, discriminator, localizer_backend=None,
                                     tau_range=array([1, 2, 3, 4, 5, 6, 7, 8, 9]), target_r_square='auto',
                                     r_metric='acc', activation='tanh+relu', save_path=False)
```

Bases: object

class for discriminative feature detection for deep learning models.

#### Parameters

##### input\_shape

[{tuple-like} (shape of the feature/image)] For example, in MNIST dataset input\_shape = (28, 28, 1).

##### localizer\_backend: {keras-defined neural network}

A backend neural network before reshape and Truncated ReLU activation.

##### discriminator: {keras-defined neural network}

A pretrained neural network needs to be explained.

**tau\_range**

[[list-like]] List of tau to define the localizers.

**target\_r\_square: {float, [0,1]}**

A target R\_square to be explained.

**R\_square: {list-like}**

Records for R\_square values based on a dataset.

**DA\_plot**(X, y, demo\_ind=None, threshold=None, plt1\_params={'cmap': 'binary'}, plt2\_params={'cmap': 'OrRd'})

Plots data-adaptive detected region for the fitted localizer.

**Parameters****X**

[[array-like] of shape (n\_samples, dim\_features)] Instances matrix/tensor, where n\_samples is the number of samples and dim\_features is the dimension of the features.

**y**

[[array-like] of shape (n\_samples,)] Output vector/matrix relative to X.

**demo\_ind**

[[array-like] of shape (num\_instance, num\_labels) default=None]

**threshold**

[[array-like] or float, default=None] threshold to truncate the small detected pixels

**R\_sqaure\_path()**

Plot solution path for the proposed method wrt tau\_range

**R\_square(X, y)**

Report R\_square for the fitted localizer based on a given dataset

**Parameters****X**

[[array-like] of shape (n\_samples, dim\_features)] Instances matrix/tensor, where n\_samples is the number of samples and dim\_features is the dimension of the features.

**y**

[[array-like] of shape (n\_samples,)] Output vector/matrix relative to X.

**build\_combined**(optimizer=<keras.optimizers.optimizer\_v2.adam.Adam object>)

Building a localizer and a combined model for the proposed framework

**Parameters****localizer: {keras-defined neural network}**

A neural network for localizer.

**optimizer: {keras-defined optimizer: ``tensorflow.keras.optimizers``, default = 'SGD(lr=.0005)'**

A optimizer used to train the localizer.

**build\_localizer**(tau=10.0, max\_value=1.0)

Building a localizer for the proposed framework

**Parameters****tau: {float}**

The magnitude of the localizer.

**max\_value:** {float, (0, 1]}

The maximum proportion of the localizer.

**fit**(*X\_train*, *y\_train*, *fit\_params*, *datagen=None*, *demo\_ind=None*, *X\_test=None*, *y\_test=None*, *optimizer=<keras.optimizers.optimizer\_v2.gradient\_descent.SGD object>*)

Fitting the localizer based on a given dataset.

#### Parameters

##### **X\_train**

[{array-like} of shape (n\_samples, dim\_features)] Instances matrix/tensor, where n\_samples is the number of samples and dim\_features is the dimension of the features.

##### **y\_train**

[{array-like} of shape (n\_samples,)] Output vector/matrix relative to X.

##### **X\_test**

[{array-like} of shape (n\_samples, dim\_features), default = None] Instances features to compute the r\_square. If None, X\_test = X\_train

##### **y\_test**

[{array-like} of shape (n\_samples,), default = None] Output to compute the r\_square. If None, y\_test = y\_train

##### **localizer**

[{keras-defined neural network}] A neural network for localizer before Truncated RELU activation.

##### **fit\_params:** {dict of fitting parameters}

See **keras fit**: (<https://keras.rstudio.com/reference/fit.html>), including **batch\_size**, **epoch**, **callbacks**, **validation\_split**, **validation\_data**, and so on.

##### **demo\_ind**

[{array-like} default=None] The index set for demonstrated instances.

**optimizer:** {keras-defined optimizer: ``tensorflow.keras.optimizers``, default = 'SGD(lr=.0005)'}  
A optimizer used to train the localizer.

#### **locate**(X)

Return the localized discriminative features by the fitted localizer.

#### Parameters

##### **X**

[{array-like} of shape (n\_samples, dim\_features)] Instances matrix/tensor, where n\_samples is the number of samples and dim\_features is the dimension of the features.

**path\_plot**(*threshold=None*, *plt1\_params={'cmap': 'binary'}*, *plt2\_params={'cmap': 'OrRd'}*)

Plots generalized partial R values and its corresponding images wrt tau\_range.

#### Parameters

##### **threshold**

[{array-like} or float] threshold to truncate the small detected pixels

##### **plt1\_params**

[{dict-like}] dict for imshow for X\_demo

##### **plt2\_params**

[{dict-like}] dict for imshow for X\_diff\_demo



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